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COMMUNICATION DEVICE, COMMUNICATION METHOD, PROGRAM, AND
STORAGE MEDIUM

BACKGROUND OF THE INVENTION

1. Field of the Invention

The present invention relates to a communication device, a communication method, a program, and a storage medium. More particularly, the present invention relates to a communication device, a communication method, a program, and a storage medium storing a program, which allow multiple access in UWB (ultra wideband) communication.

2. Description of the Related Art

UWB communication is also called impulse radio communication and is expected to find various applications, as discussed for example, in "Impulse radio: How it works" by M. Z. Win and R. A. Scholtz (IEEE Communication Letters, Vol. 2, pp. 36-38, Feb, 1998 (hereinafter, this literature will be denoted as "Ref. 1")), "UWB waveforms and coding for communications and radar" by L Fullerton (Proc. IEEE Telecommunications Conf., pp. 139-141, Mar. 26-27, 1991 (hereinafter, this literature will be denoted as "Ref. 2")), and "Answers to questions posed by Bob Lucky, Chairman of the FCC's Technical Advisory Committee (e-mail correspondence, <http://ultra.usc.edu./ulab>, June 29, 1999 (hereinafter, this literature will be denoted as "Ref. 3"))).

The UWB communication technology has many advantages that stem from its ultra-wideband nature, as described in, for example, "On the robustness of ultra-wideband width signals in dense multipath environments" by M. Z. Win and R. A. Scholtz (IEEE Communication Letters, Vol. 2, pp. 51-53, Feb., 1998 (hereinafter, this literature will be denoted as "Ref. 4")), and "On the analysis of UWB communication channels" by J. M. Cramer, R. A. Scholtz, and M. Z. Win (Proc. IEEE Military Communications Conf., pp. 1191-1195, Oct. 31 to Nov. 3, 1999 (hereinafter, denoted as "Ref. 5"))). More specifically, it can penetrate walls, experience significantly less fading, offer extremely fine time-resolution, and deliver large processing gains.

In particular, the absence of a carrier signal in the UWB communication obviates the need for radio frequency (RF) or intermediate frequency (IF) circuits. This allows reductions in device size and power consumption.

These characteristics of the UWB communication technology give it substantial advantages over conventional narrowband, wideband and infrared wireless communication

systems.

Potential applications of the UWB communication include wireless local area networks (LAN), information distribution systems for use in a medical application or the like, outdoor or indoor wireless multiple-access communication systems, ranging devices, and other many applications, as described in, for example, "Catching the wave; Breakthroughs in wireless technology" by J. S. Gage (MD Computing: The Leading Edge in Medical and Healthcare Informatics, Vol. 16, March/April 1999 (hereinafter, denoted as "Ref. 6")), and "Ultra-wideband width time-hopping spread-spectrum impulse radio for wireless multiple-access communications" by M. Z. Win and R. A. Scholtz (IEEE Trans. Communications, Vol. 48, pp. 679-691, Apr., 2000 (hereinafter, denoted as "Ref. 7")).

There is a great need for applying the UWB communication technology to multiple-access (multi-user) communication with a plurality of communication terminals. The idea of applying UWB to multiple-access communication is discussed in, for example, "Multiple access with time-hopping impulse modulation" by R. A. Scholtz (Proc. IEEE Military Communications Conf. (Boston, U.S.), pp. 447 - 450, Oct. 11-14, 1993 (hereinafter, denoted as "Ref. 8")), and "Multiple-access performance limits with time hopping and pulse position modulation" by F. Ramirez-Mireles and R. A. Scholtz (Proc. IEEE Military Communications Conf., pp. 529-

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533, Oct. 18-21, 1998 (hereinafter, denoted as "Ref. 9")).

UWB multiple-access communication systems proposed in Refs. 7 to 9 are conceptually similar to asynchronous code-division multiple-access (CDMA) systems in certain aspects. Transmitted signals of each user (signals transmitted from each communication terminal) share a common spectrum, and the set of signaling waveforms across all users are not necessarily orthogonal.

The multiple-access capability of a UWB system is primarily determined by the processing gain that is given by the pulse bandwidth to the pulse (or symbol) repetition frequency (RPF) ratio. In the UWB communication, its very wide frequency bandwidth results in a high processing gain. The UWB communication technology is very different from the CDMA communication technology in that the high processing gain of the UWB communication allows it to be advantageously employed in applications in which power is limited.

In the literatures Ref. 1 and Refs. 7 to 9, it is proposed to realize multiple-access UWB communication by time-hopping the timing of transmitting pulse-position-modulated signals of respective users on the basis of a time-hopping sequence indicated by a pseudorandom number.

Herein, the "pulse position modulation" refers to modulation of pulse positions depending on data to be transmitted. For example, a unit period with a

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predetermined length is assigned to one symbol, and each period is divided into M intervals. A pulse is placed in one of the M intervals, at a position corresponding to data to be transmitted. The "time hopping" refers to an operation of, rather than transmitting symbols (unit periods) at fixed intervals, randomly shifting the transmission timing from the fixed intervals.

In the proposed UWB multiple-access communication techniques, each receiving device includes a single-user demodulator for detecting the pulse position, in each unit period, of a pulse-position-modulated signal.

The single-user demodulator includes a filter bank including filters for matching the received signal with pulses at possible positions in unit periods, and a detector for detecting a filter that provides a highest output among the filters of the filter bank, and employing, as demodulated data, a value corresponding to a pulse position that is matched with the received signal by the filter that is determined to provide the highest output.

Ideally, in the multiple-access communication, there is no overlap among pulses of signals transmitted from users. Under such an ideal condition, the single-user demodulator can function as an ideal demodulator for demodulating a pulse-position-modulated signal in an environment including additive white Gaussian noise. In this case, the single-

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user demodulator may be constructed in a similar fashion to a single-user matched filter for detection in CDMA systems, as described, for example, in "Multiuser detection for CDMA systems" by A. Duel-Hallen, J. Holtzman and Z. Zvonar (IEEE Personal Communications Magazine, Vol. 2, pp. 46-58, Apr., 1995 (hereinafter, denoted as "Ref. 10")), "Multi-user detection for DS-CDMA communications", by S. Moshavi (IEEE Communications Magazine, Vol. 34, pp. 124-136, Oct., 1996 (hereinafter, denoted as "Ref. 11")), and "Multiuser Detection" by S. Verdu (Cambridge University Press, 1998 (hereinafter, denoted as "Ref. 12"))).

However, in practical multiple-access communication systems, interference occurs among signals transmitted from users (hereinafter, such interference will be referred to as multiple-access interference), and multiple-access interference (MAI) is generally not Gaussian. The conventional single-user modulator is no longer optimal in such an environment in which MAI can occur.

MAI increases with the number of multiple-access users, and the increase in MAI causes various adverse effects on the single-user demodulator. When data is transmitted at a high rate, the resultant high pulse repetition frequency causes a reduction in the processing gain and thus an increase in MAI.

In view of the above, it is an object of the present

invention to provide a high-performance demodulator for use in UWB multiple-access communication.

SUMMARY OF THE INVENTION

According to an aspect of the present invention, there is provided a communication device comprising correlation calculation means for calculating the correlation between a received signal corresponding to signals transmitted from a plurality of communication terminals by means of UWB (ultra wideband) communication and pulses at possible positions in a signal transmitted from each communication terminal; and demodulation means for demodulating data transmitted from the respective communication terminals on the basis of the correlation, taking into account interference among the signals transmitted from the communication terminals.

According to another aspect of the present invention, there is provided a communication method comprising the steps of calculating the correlation between a received signal corresponding to signals transmitted from a plurality of communication terminals by means of UWB (ultra wideband) communication and pulses at possible positions in a signal transmitted from each communication terminal; and demodulating data transmitted from the respective communication terminals on the basis of the correlation, taking into account interference among the signals

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transmitted from the communication terminals.

According to still another aspect of the present invention, there is provided a program comprising the steps of calculating the correlation between a received signal corresponding to signals transmitted from a plurality of communication terminals by means of UWB (ultra wideband) communication and pulses at possible positions in a signal transmitted from each communication terminal; and demodulating data transmitted from the respective communication terminals on the basis of the correlation, taking into account interference among the signals transmitted from the communication terminals.

According to still another aspect of the present invention, there is provided a storage medium storing program comprising the steps of calculating the correlation between a received signal corresponding to signals transmitted from a plurality of communication terminals by means of UWB (ultra wideband) communication and pulses at possible positions in a signal transmitted from each communication terminal; and demodulating data transmitted from the respective communication terminals on the basis of the correlation, taking into account interference among the signals transmitted from the communication terminals.

That is, in the communication device, the communication method, and the program according to the present invention,

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the correlation is calculated between the received signal corresponding to the signals transmitted from a plurality of communication terminals by means of UWB (Ultra WideBand) communication technology and pulses at possible positions in the transmitted signals from the respective communication terminals, and the received signal is demodulated into original data issued by the communication terminals on the basis of the calculated correlation taking into account interference among the transmitted signals from the respective communication terminals.

BRIEF DESCRIPTION OF THE DRAWINGS

Fig. 1 is a diagram illustrating an example of a construction of a UWB communication system according to an embodiment of the present invention;

Fig. 2 is a block diagram illustrating an example of a construction of a communication device;

Fig. 3 is a block diagram illustrating an example of a construction of a UWB demodulator;

Fig. 4 a diagram illustrating a signal transmitted by means of UWB communication technology;

Fig. 5 is a block diagram illustrating an example of a construction of a correlator;

Fig. 6 is a block diagram illustrating an example of a construction of a correlator bank;

Fig. 7 is a block diagram illustrating another example of a construction of a correlator;

Fig. 8 is a block diagram illustrating an example of a construction of a single-user demodulator;

Fig. 9 is a block diagram illustrating an example of a construction of a symbol detector functioning as an optimum demodulator;

Fig. 10 is a flow chart showing the process performed by the UWB demodulator functioning as the optimum demodulator;

Fig. 11 is a block diagram illustrating a first example of a construction of a symbol detector functioning as a suboptimum demodulator;

Fig. 12 is a flow chart showing the process performed by the UWB demodulator functioning as the suboptimum demodulator shown in Fig. 11;

Fig. 13 is a block diagram illustrating a second example of a construction of a symbol detector functioning as a suboptimum demodulator;

Fig. 14 is a flow chart showing the process performed by the UWB demodulator functioning as the suboptimum demodulator shown in Fig. 14;

Fig. 15 is a graph illustrating a simulation result;

Fig. 16 is a graph illustrating a simulation result;
and

Fig. 17 is a block diagram illustrating an example of a construction of a computer according to an embodiment of the present invention.

DESCRIPTION OF THE PREFERRED EMBODIMENTS

Fig. 1 illustrates an embodiment of a UWB communication system according to the present invention (herein, the term "system" refers to a logical set of apparatuses, the physical locations of which may or may not be within a single physical enclosure).

In the embodiment shown in Fig. 1, the UWB communication system includes $K + 1$ communication devices $1_1, 1_2, \dots, 1_{k+1}$. Each communication device 1_k modulates data to be transmitted by means of, for example, pulse position modulation and transmits the modulated signal as a radio transmission signal using a UWB communication technique through a transmission path 2. Each communication device 1_k also receives signals transmitted from the other communication devices 1_k through the transmission path 2 and demodulates the received signals into original data. Hereinafter, a user of the communication device 1_k is denoted as a user #k.

In the following discussion, among $K + 1$ communication devices $1_1, 1_2, \dots, 1_{k+1}$, a communication device 1_{k+1} is taken as an example, and the operation thereof is described. The

communication device l_{k+1} is capable of communicating with any of the other communication devices l_1, l_2, \dots, l_k of K users #1, #2, ..., #K by means of multiple access communication, in which a received signal corresponding to a signal transmitted from each user is demodulated into original data issued by the user.

As with the communication device l_{k+1} , each of the other communication devices l_1, l_2, \dots, l_k is capable of communicating with the other K communication devices by means of multiple access communication, although the communication device l_{k+1} is taken as an example in the following discussion.

The UWB communication system such as that shown in Fig. 1 may be applied to, for example, a wireless LAN system or the like.

Fig. 2 illustrates an example of a construction of the communication device l_{k+1} shown in Fig. 1. Each of the other communication devices l_1, l_2, \dots, l_k may be constructed in a similar manner to the communication device l_{k+1} .

The communication device l_{k+1} includes a UWB modulator 11, an antenna 12, and a UWB demodulator 13.

Data to be transmitted is supplied to the UWB modulator 11. The UWB modulator 11 modulates the supplied data by means of pulse position modulation in which positions of pulses (impulses) are determined in accordance with the

supplied data. The resultant modulated signal is supplied to the antenna 12 while performing time hopping.

Upon receiving the modulated signal from the UWB modulator 11, the antenna 12 transmits the modulated signal in the form of a radio wave. The antenna 12 also receives a radio wave from other communication devices 1 and supplies the received signal to the UWB demodulator 13.

The UWB demodulator 13 demodulates the received signal supplied from the antenna 12 in a manner described later and outputs the resultant demodulated data.

Fig. 3 shows an example of a construction of the UWB demodulator 13 shown in Fig. 2.

The UWB demodulator 13 includes a correlator 21 and a symbol detector 22.

The received signal is supplied from the antenna 12 to the correlator 21. The correlator 21 calculates the correlation of the received signal with respect to possible pulse positions for signals transmitted from the respective communication terminals 1_1 to 1_k . The resultant correlation is supplied to the symbol detector 22. On the basis of the correlation supplied from the correlator 21, and taking into account interference among the signals transmitted from the communication terminals 1_1 to 1_k , the symbol detector 22 demodulates the received signal into original data issued by the communication devices 1_1 to 1_k .

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The process performed by the UWB demodulator 13 shown in Fig. 3 is described in further detail below on the basis of a model of a multi-user UWB communication system.

A multiple-access model in an additive white Gaussian noise environment has been proposed, for example, in the literatures Refs. 1 and 7 cited above. The multi-user UWB communication system can be modeled in part on the basis of that given in Ref. 1 or 7. However, the primary difference is the introduction of an equivalent vector model as described in "Sequence detection and equalization for pulse-position modulation" by J. R. Barry (Proc. IEEE Intl. Conf. Communications, pp. 1561-1565, May 1-5, 1994 (hereinafter denoted as "Ref. 13"))).

Note that the equivalent vector model can be applied not only to the pulse position modulation but also to orthogonal modulation schemes. That is, although it is assumed that pulse position modulation is employed in the present embodiment, the process described below may also be applied to orthogonal modulation.

In the multiple-access model in an environment including additive white Gaussian noise, a received signal $r(t)$ from user $\#K + 1$ (communication device 1_{k+1}) can be expressed using transmitted signals $s^{(k)}(t)$ from user $\#k$ (communication devices 1_k), as described below:

$$r(t) = \sum_{k=1}^K s^{(k)}(t) + n(t) \quad (1)$$

In this equation (1), t denotes time, and $n(t)$ denotes zero-mean white Gaussian noise with a power spectral density of $N_0/2$, where N_0 is the mean power of white Gaussian noise.

The transmitted signal $s^{(k)}(t)$ of user # k in equation (1) can be expressed as follows:

$$s^{(k)}(t) = \sqrt{E_s^{(k)}} \sum_{n=1}^N \sum_{m=1}^M b_n^{(k,m)} a^m(t - nT_s - T_n^{(k)}) \quad (2)$$

wherein $E_s^{(k)}$ denotes symbol energy of the transmitted signal from user # k . Herein, it is assumed that $E_s^{(1)} = E_s^{(2)} = \dots, E_s^{(k)} = E_s$, although the above assumption is not necessarily needed, and the invention may also be applied to non-uniform signal energies.

In equation (2), N denotes the number of symbols transmitted by each user # k (the number of symbols detected at a time in detection of a symbol sequence), and T_s denotes a symbol transmission repetition period for each user # k . Thus, $1/T_s$ represents the symbol rate, which is generally referred to as the pulse repetition frequency (RPF) in the art of UWB communication.

In equation (2), M denotes the unit symbol size. In the case of the pulse position modulation, M indicates the number of intervals included in each unit period with a predetermined length. Positions corresponding to respective

M intervals included in each unit period are called chips (strictly speaking, M intervals are called chips). In the case where each symbol includes M chips and a pulse is placed only in one of the M chips depending on data to be transmitted, the number of bits transmitted per symbol is given by $\log_2 M$.

In equation (2), $b_n^{(k,m)}$ becomes 1 when a pulse is placed at an mth position of an nth symbol of the transmitted signal of user #k, and becomes 0 when no pulse is placed at that position. Thus, a vector b_n^k including elements $b_n^{(k,m)}$, such as $[b_n^{(k,1)}, b_n^{(k,2)}, \dots, b_n^{(k,M)}]^T$ (superscript T represents transpose), represents an nth symbol of the transmitted signal from the user #k.

Herein, it is assumed that only one of M elements $b_n^{(k,m)}$ in the vector $b_n^{(k)}$ is 1, while the remaining M - 1 elements are 0. That is, a pulse is placed only at one of M positions in each unit period, depending on data to be transmitted. More specifically, when j (j = 0, 1, ..., M - 1) is data to be transmitted, only (j+1)th element $b_n^{(k,j+1)}$ is set to 1, and the other elements are set to 0. Note that, alternatively, a plurality of pulses may be placed in each unit period depending on data to be transmitted.

In equation (2), $a^{(m)}(t)$ represents the waveform of a pulse at a position m. The pulse $a^{(m)}(t)$ has unit signal energy and satisfies the following equation.

$$\int_{-\infty}^{\infty} a^{(m)}(t) a^{(m)}(t) dt = \delta_{m,m} \quad (3)$$

where $\delta_{m,m}$ is the kronecker delta function.

More specifically, the pulse $a^{(m)}(t)$ is represented by the following equation:

$$a^{(m)}(t) = w_{rec}(t - mT_p) \quad (4)$$

As can be seen from equation (4), the possible positions at which pulses $a^{(m)}(t)$ can be placed in each unit period are spaced from each other by a time interval T_p . In other words, the time T_p represents time intervals at which each unit period is divided into chips (hereinafter, T_p will be referred to as a chip interval).

The signal $w_{rec}(t)$ that defines the pulse $a^{(m)}(t)$ has a very short pulse waveform with a width equal to or smaller than 1 ns. For example, as described in Ref. 7, the signal $w_{rec}(t)$ can be given by the following equation:

$$w_{rec}(t) = \sqrt{\frac{8}{3}} [1 - 4\pi(\frac{t}{\tau_{uwb}})^2] \exp[-2\pi(\frac{t}{\tau_{uwb}})^2] \quad (5)$$

wherein τ_{uwb} is a parameter that determines the pulse width, and time t is in units of nano-seconds (ns). For example, when $\tau_{uwb} = 0.7531$ ns, the width of the pulse $w_{rec}(t)$ becomes about 1.5 ns, as is discussed, for example, in a paper entitled "Performance of ultra wideband time-shift-modulated signals in the indoor wireless impulse radio channel" by F. Ramirez-Mireles, M. Z. Win, R. A. Scholtz and M. A. Barnes

(Proc. Asilomar Conf. on Signal, Systems and Computers, pp. 192-196, Nov. 2-5, 1997 (hereinafter denoted as "Ref. 14")), and a paper entitled "Performance of Equicorrelated ultra-wideband pulse-position-modulated signals in the indoor wireless impulse radio channel" by F. Ramirez-Mireles and R. A. Scholtz (Proc. IEEE Pacific Pim Conf. on Communications, Computers and Signal Processings, pp. 640-644, Aug. 20-22, 1997 (hereinafter denoted as "Ref. 15"))).

Strictly speaking, the pulse width refers to a time duration during which the pulse $w_{rec}(t)$ can be regarded as existing.

In equation (5), the factor $\sqrt{(8/3)}$ has been introduced to normalize the energy of the pulse $w_{rec}(t)$ such that

$$\int_{-\infty}^{\infty} (w_{rec}(t))^2 dt = 1.$$

The correlation (autocorrelation) $\rho(t)$ among pulses $w_{rec}(t)$ is given as:

$$\rho(t) = \int_{-\infty}^{\infty} w_{rec}(t-u) w_{rec}(u) du \quad (6)$$

As described, for example, in Ref. 9, the autocorrelation $\rho(t)$ given by equation (5) can be approximated as follows:

$$\rho(t) = e^{-\alpha} \left[1 - 4\alpha + \frac{4}{3}\alpha^2 \right] \quad (7)$$

where $\alpha = \pi(t/\tau_{uwb})^2$.

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The TH time $T_n^{(k)}$ is represented using $T^{(k)}$ and $T'_n{}^{(k)}$ such that $T_n^{(k)} = T^{(k)} + T'_n{}^{(k)}$. Herein, $T^{(k)}$ can take a value within the range of $0 \leq T^{(k)} < T_s$ and represents a delay of a symbol transmitted from user #k relative to a symbol delay $T^{(1)}$ for user #1 (that is, $T^{(1)} = 0$). Time $T'_n{}^{(k)}$ represents pseudo noise that determines time hopping and can take a value within the range of $0 \leq T'_n{}^{(k)} < T_{TH,max}$. Herein, it is required that $T_{TH,max} \leq T_s$, and it is also required that the minimum difference $T_s - T_{TH,max}$ should be smaller than a sample-and-hold time of the S/H (sample-and-hold) circuit 55 in a correlator 41_m (Fig. 7) that will be described later and also than an interval between a pulse placed in a certain symbol and a pulse placed at a next symbol.

Herein, for the purpose of simplicity, it is assumed that $T_{\text{TH,max}} = T_s$ and it is also assumed that the time-hopping sequence $\{T_n^{(k)}\}$ is modeled as a sequence of independent and

identically distributed continuous random variables each uniformly distributed over the range from (equal to or greater than) 0 to (smaller than) $T_{TH,max}$. In practice, however, the time-hopping sequence $\{T^{(k)}\}$ are discretized over chip intervals.

As can be seen from equation (2), a signal $s^{(k)}(t)$ is transmitted from a user #k as shown in Fig. 4A.

In Fig. 4A, a symbol #n is transmitted from the user #k when a period of time equal to $T_s + T_n^{(k)}$ has elapsed since the transmission of a previous symbol #n-1.

In the symbol #n, as shown in Fig. 4B, a pulse represented by $\sqrt{(E_s^{(k)})}w_{rec}(t)$ is placed at a position m of M positions spaced from each other by T_p , wherein the position m depends on the data being transmitted.

Referring again to Fig. 3, the correlator 21 calculates the correlation of the received signal $r(t)$ represented by equation (1) with respect to possible pulse positions for signals transmitted from the respective users #1 to #K.

For a certain user #k' of the plurality of users #1 to #K, a pulse placed at an m'th position in an n'th symbol (such a pulse is referred to as a local pulse) of a signal transmitted from the user #k' can be represented as $a^{(m')}(t - n'T_s - T_n^{(k')})$. Thus, for the user #k', the correlator 21 calculates the correlation $y_n^{(k',m')}$ in accordance with the following equation:

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(8)

For the user k' , the correlation $y_n^{(k', m')}$ represented by equation (8) is calculated for all positions m' . Herein, we introduce an $M \times 1$ vector $y_n^{(k')}$ whose elements are given by correlations $y_n^{(k', 1)}, y_n^{(k', 2)}, \dots, y_n^{(k', M)}$ calculated for the respective positions $m' = 1, 2, \dots, M$. That is, the $M \times 1$ vector $y_n^{(k')}$ can be represented as follows:

(9)

Because symbol transmission between a certain user and another user is performed asynchronously, the correlations $y_{n'}^{(1)}, y_{n'}^{(2)}, \dots, y_{n'}^{(k')}$ associated with the respective users outputted from the correlator 21 are not necessarily deterministic with respect to the time phase, and the correlations should be treated as stochastic variables. Therefore, hereinafter, values (such as $y_{n'}^{(k',m')}$ or $y_{n'}^{(k')}$) outputted from the correlator 21 will be referred to as correlation statistics.

The correlation statistic $y_n^{(k', m')}$ in equation (8) can be determined by substituting the received signal $r(t)$ given by equation (1) into equation (8). Thus, the correlation statistic $y_n^{(k', m')}$ is given as:

(10)

where $\rho^{n',k',m'}$ is the correlation vector between the local pulse $a(m')(t - n'T_s - T_{n'}^{(k')})$ and the signals $s^{(1)}(t)$ to $s^k(t)$

transmitted from the users #1 to #K, and the correlation vector $\rho^{n',k',m'}$ can be represented in the form of an $NKM \times 1$ vector as shown below:

$$\rho^{n',k',m'} = [\rho_1^{n',k',m'}, \dots, \rho_N^{n',k',m'}]^T \quad (11)$$

The correlation vector $\rho^{n',k',m'}$ in equation (11) includes N elements in the form of vectors $\rho_n^{n',k',m'}$. Each vector $\rho_n^{n',k',m'}$ is a correlation vector between a local pulse $a^{m'}(t - n'T_s - T_{n,(k')})$ and an nth symbol in signals $s^{(1)}(t)$ to $s^{(k)}(t)$ transmitted from users #1 to #K, and is represented in the form of a $KM \times 1$ vector as shown below:

$$\rho_n^{n',k',m'} = [\rho_{n,1}^{n',k',m'}, \dots, \rho_{n,K}^{n',k',m'}]^T \quad (12)$$

The correlation vector $\rho_n^{n',k',m'}$ in equation (12) includes N elements in the form of vectors $\rho_{n,k}^{n',k',m'}$. Each vector $\rho_{n,k}^{n',k',m'}$ is a correlation vector between a local pulse $a^{(m')}(t - n'T_s - T_{n,(k')})$ and an nth symbol of a signal $s^{(k)}(t)$ transmitted from a user #k, and is represented in the form of an $M \times 1$ vector as shown below:

$$\rho_{n,k}^{n',k',m'} = [\rho_{n,k,1}^{n',k',m'}, \dots, \rho_{n,k,M}^{n',k',m'}]^T \quad (13)$$

Each element $\rho_{n,k,m}^{n',k',m'}$ of the correlation vector $\rho_{n,k}^{n',k',m'}$ in equation (13) represents the correlation between a local pulse $a^{(m')}(t - n'T_s - T_{n,(k')})$ and a pulse at an mth position of an nth symbol of a signal $s^{(k)}(t)$ transmitted from a user #k, and can be calculated in accordance with equation (14) shown below, wherein the correlation $\rho_{n,k,m}^{n',k',m'}$ in this equation (14) can be calculated in accordance with equations (4) to

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(7) described above.

$$\rho_{n,k,m}^{n',k',m'} = \int_{-\infty}^{\infty} a^{(m)}(t - nT_s - T_n^{(k)}) a^{(m')} (t - n'T_s - T_n^{(k')}) dt \quad (14)$$

In equation (10), the matrix A is a $KMN \times KMN$ diagonal matrix representing the signal energies for all symbols and all users, and can be represented as follows:

$$A = \text{diag}(A_1^T, \dots, A_N^T) \quad (15)$$

where each element A_n of the matrix A is a $KM \times 1$ vector, and $\text{diag}(A_n)$ denotes a diagonal matrix whose diagonal elements are given by vectors A_n .

Each vector A_n that is an element of the matrix A in equation (15) can be represented by equation (16) shown below.

$$A_n = [A_n^{(1)T}, \dots, A_n^{(K)T}]^T \quad (16)$$

In equation (16), each element $A_n^{(k)}$ of the vector A_n is a $M \times 1$ vector having identical elements $E_s^{(k)}$ as shown in equation (17).

$$A_n^{(k)} = [E_s^{(k)}, E_s^{(k)}, \dots, E_s^{(k)}]^T \quad (17)$$

In equation (10), the vector b is an $NKM \times 1$ vector given by equation (18) representing possible pulse positions for a symbol of each user, that is, possible symbol values.

$$b = [b_1^T, \dots, b_N^T]^T \quad (18)$$

Each element b_n of the vector b in equation (18) is a $KM \times 1$ vector representing possible values of an n th symbol transmitted from each user, and is given by equation (19)

shown below.

$$b_n = [b_n^{(1)T}, \dots, b_n^{(K)T}]^T \quad (19)$$

Each element b_n^k of the vector b_n in equation (19) is an $M \times 1$ vector representing possible values of an n th symbol transmitted from a user k , and is given by equation (20) shown below.

$$b_n^{(k)} = [b_n^{(k,1)}, \dots, b_n^{(k,M)}]^T \quad (20)$$

In equation (10), $\eta^{n',k',m'}$ is a Gaussian random variable with a mean value of 0 and a variance of $N_0/2$.

If the collection of correlation statistics $y_n^{(k')}$ for all symbols and all users, which are represented by equation (9) and outputted from the correlator 21, is denoted by a vector y , then equation (10) can be rewritten using this correlation statistic y as follows:

$$y = RAb + \eta \quad (21)$$

where the vector b is defined in equations (18) to (20).

The vector y in equation (21) is a $KMN \times 1$ vector including N vectors given by the following equation:

$$y = [y_1^T, \dots, y_N^T]^T \quad (22)$$

In equation (22), each element of the vector y , that is, the vector y_n , represents a correlation statistic of an n th symbol for all users, and the vector y_n is a $KM \times 1$ vector represented by the following equation:

$$y_n = [y_n^{(1)T}, \dots, y_n^{(K)T}]^T \quad (23)$$

In equation (23), the vector y_n includes elements in

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the form of vectors $y_n^{(k')}$ defined in equation (9).

In equation (21), R is an $NKM \times NKM$ correlation matrix, which is defined as follows:

$$R = [\rho^{1^T}, \dots, \rho^{N^T}]^T \quad (24)$$

In equation (24), each element $\rho^{n'}$ of the correlation matrix R is a $KM \times NKM$ matrix representing the correlation between a local pulse and an n' th symbol for all users, and is given by the following equation:

$$\rho^{n'} = [\rho^{n',1^T}, \dots, \rho^{n',K^T}]^T \quad (25)$$

In equation (25), each element $\rho^{n',k'}$ of the matrix $\rho^{n'}$ is an $M \times NKM$ matrix representing a local pulse and an n' th symbol of a signal transmitted from a user $\#k'$, and is given by the following equation:

$$\rho^{n',k'} = [\rho^{n',k',1^T}, \dots, \rho^{n',k',M^T}]^T \quad (26)$$

In equation (26), each element $\rho^{n',k',m'}$ of the matrix $\rho^{n',k'}$ is defined in equation (11).

η in equation (21) corresponds to $\eta^{n',k',m'}$ in equation (10) and defined by a vector (noise vector) given by the following equation:

$$\eta = [\eta_1^T, \dots, \eta_N^T]^T \quad (27)$$

where the vector $\eta_{n'}$ is defined as follows:

$$\eta_{n'} = [\eta_{n'}^{(1)^T}, \dots, \eta_{n'}^{(K)^T}]^T \quad (28)$$

where the vector $\eta_{n'}^{(k')}$ is defined as follows:

$$\eta_{n'}^{(k')} = [\eta_{n',k',1}, \dots, \eta_{n',k',M}]^T \quad (29)$$

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Note that elements of $\eta_n^{k'}$ in equation (29) are given by $\eta^{n',k',m'}$ in equation (10).

The correlator 21 shown in Fig. 3 calculates the correlation statistic y in equation (21) (in practice, the correlator 21 calculates the correlation statistic in accordance with equation (8), which results in the same correlation statistic according to equation (21). To this end, as shown in Fig. 5, the correlator 21 includes as many K correlator banks 31_1 to 31_k as there are multi-access users and also includes switches 32_1 to 32_k disposed at the outputs of the respective correlator banks 31_1 to 31_k .

The received signal $r(t)$ is supplied to each correlator bank 31_k . The correlator bank 31_k calculates the correlator statistic $y_n^{(k')}$ in equation (9) using the received signal $r(t)$ and the local pulse $a^{(m')}(t - n'T_s - T_{n'}^{(k')})$ in accordance with equation (8).

The correlation statistic $y_n^{(k')}$ outputted from the correlator bank 31_k is supplied to the switch 32_k . The switch 32_k is normally in an off-state and is turned on at a time $t = (n' + 1)T_s$ so that the correlation statistic $y_n^{(k')}$ outputted from the correlator bank 31_k is supplied to the symbol detector 22 (Fig. 3) disposed at the following stage via the switch 32_k at $t = (n' + 1)T_s$.

Fig. 6 shows an example of a construction of the correlator bank 31_k shown in Fig. 5.

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The correlator bank 31_k includes as many correlators 41_1 to 41_m as there are M possible pulse positions within a unit period during which a symbol is transmitted.

The received signal $r(t)$ is supplied to each correlator 41_m . The correlator 41_m calculates the correlator statistic $y_n^{(k',m')}$ in equation (8) using the received signal $r(t)$ and the local pulse $a^{(m')}(t - n'T_s - T_n^{(k')})$ in accordance with equation (8).

Fig. 7 shows an example of a construction of the correlator 41^m shown in Fig. 6.

A TH (time-hopping) time generator 51 generates a TH time $T_n^{(k')}$ and supplies it to a pulse generator 52. On the basis of the TH time $T_n^{(k')}$ supplied from the TH time generator 51, the pulse generator 52 generates a local pulse $a^{(m')}(t - n'T_s - T_n^{(k')})$ and supplies it to a multiplier 53.

In addition to the local pulse $a^{(m')}(t - n'T_s - T_n^{(k')})$ supplied from the pulse generator 52, the received signal $r(t)$ is also supplied to the multiplier 53. The multiplier 53 calculates the product of the received signal $r(t)$ and the local pulse $a^{(m')}(t - n'T_s - T_n^{(k')})$ thereby determining $r(t)a^{(m')}(t - n'T_s - T_n^{(k')})$ that is to be integrated with respect to time as shown in equation (8). The result is supplied to an integrator 54.

The integrator 54 integrates the output of the multiplier 53 with respect to time in accordance with

equation (8). The resultant integral value to an S/H circuit 55.

The S/H circuit 55 samples and holds the output of the integrator 54 at a time indicated by the TH time $T_n^{(k')}$. The sampled and held value is outputted as the correlation statistic $y_n^{(k',m')}$ represented in equation (8).

In the case where the UWB demodulator 13 shown in Fig. 3 is constructed as a single-user demodulator, the correlator 21 includes, as shown in Fig. 8, only one correlator 61 similar to the correlator bank 31_k shown in Fig. 6.

In this case, the output of the correlator 21 represents the correlation statistic $y_n^{(k',m')}$ ($= [y_n^{(k',1)}, y_n^{(k',2)}, \dots, y_n^{(k',M)}]$) associated with only a particular user $\#k'$, and the symbol detector 22 at the following stage detects a symbol on the basis of the correlation statistic $y_n^{(k',m')}$ associated with that user $\#k'$.

In this case, because only the correlation statistic $y_n^{(k',m')}$ of the single user $\#k'$ is supplied to the symbol detector 22, it is impossible to take into account the correlation statistics for other users, that is, interference with other users, in the symbol detection. That is, the symbol detector 22 estimate a value $b'_{n^{(k',m')}} for a symbol from a user $\#k'$ without taking into account interference with other users, in accordance with a$

determination criterion given by the following equation.

$$b_{n'}^{(k',m')} = \begin{cases} 1, & \text{if } y_{n'}^{(k',m')} = \max(y_{n'}^{(k')}), \\ 0, & \text{otherwise.} \end{cases} \quad (30)$$

That is, in the case where the UWB demodulator 13 is constructed as the single-user demodulator, the symbol detector 22 detects a maximum value $y_{n'}^{(k',m(\max))}$ from the correlation statistics $y_{n'}^{(k',1)}, y_{n'}^{(k',2)}, \dots, y_{n'}^{(k',M)}$, and $m(\max)$ corresponding to the detected maximum value is outputted as demodulated data.

In contrast, in the case where the UWB demodulator 13 is constructed as an optimum multi-user demodulator (optimum detector), the symbol detector 22 may be constructed, for example, as shown in Fig. 9.

In the example shown in Fig. 9, the symbol detector 22 includes a correlation matrix calculator 71, an energy estimator 72, a symbol pattern generator 73, and a maximum-likelihood sequence detector 74.

The correlation matrix calculator 71 calculates the correlations among pulses at possible positions for signals transmitted from users in accordance with equation (14) thereby determining the correlation matrix R including the calculated correlations as represented in equation (24), and supplies the result to the maximum-likelihood sequence detector 74. In the above calculation of the correlation matrix R performed by the correlation matrix calculator 71

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The energy estimator 72 estimates the energies $E_s^{(k)}$ of the transmitted signals for respective users #k and determines the matrix A (energy matrix) including the estimated energies $E_s^{(k)}$ as elements as shown in equation (15). The resultant energy matrix A is supplied to the maximum-likelihood sequence detector 74. In the present embodiment, as described above, the energies $E_s^{(1)}, E_s^{(2)}, \dots, E_s^{(k)}$ of the signals transmitted from the respective users are assumed to have an identical value E_s .

To the maximum-likelihood sequence detector 74, the correlation statistic (vector) y outputted from the correlator 21 is also supplied in addition to the correlation matrix R outputted from the correlation matrix

calculator 71, the energy matrix A outputted from the energy estimator 72, and the pattern vector b outputted from the symbol pattern generator 73, as described earlier. Using information about these, the maximum-likelihood sequence detector 74 determines the maximum-likelihood sequence thereby determining an estimated symbol sequence (vector) $b'^{(1)}, b'^{(2)}, \dots, b'^{(k)}$ and outputs the resultant estimated symbol sequence as demodulated data.

More specifically, the maximum-likelihood sequence detector 22 determines a maximum-likelihood symbol sequence (vector) $b' = [b'^{(1)}, b'^{(2)}, \dots, b'^{(k)}]$ for the users #1 to #K, using the correlation statistic y, the correlation matrix R, the energy matrix A, and the pattern vector b, in accordance with a determination criterion given by the following equation.

$$b' = \arg \min_b \|y - RA b\|^2 \quad (31)$$

In equation (31), $\arg \min(x)$ with respect to b represents an operation of determining b that results in minimization of x.

In accordance with equation (31), of M^{KN} pattern vectors b, a vector that gives a minimum value of the norm $\|y - RA b\|^2$ is employed as the maximum-likelihood symbol sequence b'.

In the case where the UWB demodulator 13 is constructed as the optimum multi-user demodulator as shown in Fig. 9,

the UWB demodulator 13 performs a process in accordance with a procedure shown in the form of a flow chart in Fig. 10.

First, in step S1, the correlation matrix calculator 71 determines the correlation matrix R , and the energy estimator 72 determines the energy matrix A . Furthermore, the symbol pattern generator 73 determines the pattern vector b and supplies the result to the maximum-likelihood sequence detector 74.

Thereafter, in step S2, the correlator 21 determines the correlation between the received signal $r(t)$ and the local pulses. The correlation statistic y obtained as a result is supplied to the maximum-likelihood sequence detector 74.

Using the correlation statistic y , the correlation matrix R , the energy matrix A , and the pattern vector b , the maximum-likelihood sequence detector 74 determines the maximum-likelihood sequence $b' = [b'^{(1)}, b'^{(2)}, \dots, b'^{(k)}]$ for the users #1 to #K in accordance with a determination criterion given by equation (31) and outputs the result as the demodulated data.

Thereafter, the process returns to step S2 to perform the above-described operation for the next received signal $r(t)$.

Although the UWB demodulator 13 can be constructed in the form of an optimum multi-user demodulator (optimum

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detector) as described above, the UWB demodulator 13 may also be constructed in the form of a suboptimum multi-user demodulator (suboptimum detector).

That is, the UWB demodulator 13 may detect optimum symbols (sequence) from the respective users by jointly demodulating the signals from all users on the basis of all correlation statistics $y_n^{(1)}, y_n^{(2)}, \dots, y_n^{(k)}$ of all users taking into account interference among users, or may detect suboptimum symbols (sequence) by removing interference components among users (multiple-access interference) from the correlation statistics $y_n^{(1)}, y_n^{(2)}, \dots, y_n^{(k)}$ using the correlation statistics $y_n^{(1)}, y_n^{(2)}, \dots, y_n^{(k)}$ of all users.

The UWB demodulator 13 may be constructed in the form of a suboptimum multi-user demodulator, for example, using a decorrelator.

The decorrelator is analogous to a zero-forcing linear detector for intersymbol interference limited channels in single-user systems. The decorrelator projects the correlation statistic y onto a signal space having no multiple-access interference (MAI) by means of a linear transformation in accordance with equation (32) shown below thereby determining the correlation statistic y' in the signal space.

$$y' = R^{-1}y \quad (32)$$

After determining the correlation statistic y' in the

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signal space having no multiple-access interference in the above-described manner, a suboptimum symbol sequence $b'_{n'}^{(1,m)}$, $b'_{n'}^{(2,m)}$, ..., $b'_{n'}^{(k,m)}$ for the users #k to #K can be estimated in accordance with the determination criterion given by equation (30).

Fig. 11 shows an example of a construction of the symbol detector 22 in the UWB demodulator 13 constructed as a suboptimum multi-user demodulator using a decorrelator.

As with the correlation matrix calculator 71 shown in Fig. 9, a correlation matrix calculator 81 calculates the correlation matrix and supplies the result to an inverse matrix calculator 82. The inverse matrix calculator 82 calculates the inverse matrix R^{-1} of the correlation matrix R supplied from the correlation matrix calculator 81 (hereinafter, such an inverse matrix will be referred to as an inverse correlation matrix) and supplies the result to an inverse correlation calculator 83.

If the determinant of the correlation matrix R is equal to 0 or a very small value, which can occur when there is noise or a calculation error or when the correlation matrix R is not regular, the inverse matrix calculator 82 performs exception handling in which the inverse correlation matrix R^{-1} is replaced by a generalized inverse matrix with a maximum square norm.

In addition to the inverse correlation matrix R^{-1}

outputted from the inverse matrix calculator 83, the correlation statistic y outputted from the correlator 21 is also supplied to the inverse correlation calculator 83. The inverse correlation calculator 83 converts the correlation statistic y into a correlation statistic y' in a signal space including no multiple-access interference, in accordance with equation (32), that is, by means of a linear transformation using the inverse correlation matrix R^{-1} . The resultant correlation statistic y' is supplied to a maximum value detector 84.

In accordance with the determination criterion given by equation (30), the maximum value detector 84 determines the maximum value $y'_{n^{(k', m(\max))}}$ of the correlation statistics $y'_{n^{(k', 1)}}$, $y'_{n^{(k', 2)}}$, ..., $y'_{n^{(k', M)}}$ associated with the user #k in the correlation statistic y' supplied from the inverse correlation calculator 83. The maximum value detector 84 then determines $m(\max)$ at which the maximum value $y'_{n^{(k', m(\max))}}$ is obtained. Furthermore, on the basis of the determined $m(\max)$, the maximum value detector 84 estimates a suboptimum symbol sequence $b'_{n^{(k')}}$ for the user #k and outputs it as demodulated data. The maximum value detector 84 also determines and outputs demodulated data for other users in a similar manner.

In Fig. 11, the correlation matrix calculator 81, the inverse matrix calculator 82, and the inverse correlation

calculator 83 form the decorrelator.

Fig. 12 is a flow chart showing the process performed by the UWB demodulator 13 constructed in the form of the suboptimum multi-user demodulator using the decorrelator such as that shown in Fig. 11.

In the first step S11, the correlation matrix calculator 81 determines the correlation matrix R and outputs the result to the inverse matrix calculator 82. Thereafter, the process proceeds to step S12. In step S12, the inverse matrix calculator 82 determines the inverse matrix R^{-1} of the correlation matrix R and supplies the resultant inverse matrix R^{-1} to the inverse correlation calculator 83.

Thereafter, the correlator 21 determines the correlation between the received signal $r(t)$ and the local pulses and supplies the correlation statistic y obtained as a result to the inverse correlation calculator 83. In step S13, in accordance with equation (32), the inverse correlation calculator 83 determines the correlation statistic y' by mapping the correlation statistic y into a signal space including no multiple-access interference. The result is outputted to the maximum value detector 84.

In step S14, the maximum value detector 84 determines the maximum value of the correlation statistic y' supplied from the inverse correlation calculator 83 for each user in

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accordance with the determination criterion given by equation (30). Furthermore, on the basis of the maximum value, the maximum value detector 84 estimates a suboptimum symbol sequence b' for each user and outputs it as demodulated data.

Thereafter, the process returns to step S13, and the above-described operation is performed again when the correlation statistic y associated with the next received signal $r(t)$ is supplied from the correlator 21.

In the case where the UWB demodulator 13 is constructed in the form of an optimum demodulator, as described above with reference to Figs. 9 and 10, correlation matrix information is required when the correlation matrix R is calculated, and estimated energy of a signal transmitted from each user is required when the energy matrix A is calculated. In the case where the UWB demodulator 13 is constructed in the form of a suboptimum demodulator using a decorrelator as shown in Fig. 11, calculation of the energy matrix A is not needed although calculation of the correlation matrix R is required. That is, in this case, it is not needed to estimate the energy of the transmitted signal from each user.

When the WUB demodulator 13 is constructed using the decorrelator, although the correlation statistic y is mapped by the decorrelator into the signal space including no

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multiple-access interference and thus interference components are removed, a slight increase in noise occurs.

Although, in the above example, a decorrelator is used to construct the UWB demodulator 13 into the form of a suboptimum multi-user demodulator (suboptimum detector), an MMSE (Minimum Mean Square Error) detector may also be employed.

The MMSE detector converts the correlation statistic y such that the mean square error thereof becomes minimum. This allows well-balanced reductions in intersymbol interference by means of zero-forcing method and white Gaussian noise. For example, the MMSE detector for this purpose may be constructed in a similar manner to a single-user linear MMSE detector.

After conversion of the correlation statistic y using the linear MMSE detector, a suboptimum symbol sequence $b'_{n^{(1,m)}}$, $b'_{n^{(2,m)}}$, ..., $b'_{n^{(k,m)}}$ for the users #k to #K can be estimated in accordance with the determination criterion given by equation (30).

Fig. 13 shows an example of a construction of the symbol detector 22 in the UWB demodulator 13 constructed as a suboptimum multi-user demodulator using a linear MMSE detector.

As with the correlation matrix calculator 71 shown in Fig. 9, a correlation matrix calculator 91 calculates the

In addition to the correlation matrix R outputted from the correlation matrix calculator 91, the energy matrix A outputted from the energy estimator 92 and the correlation statistic y outputted from the correlator 21 are also supplied to the mean square error calculator 93. The mean square error calculator 93 converts the correlation statistic y outputted from the correlator 21 into y' with a minimized mean square error using a conversion matrix expressed using the correlation matrix R and the energy matrix A as shown in equation (33) and supplies the result y' to the maximum value detector 94.

(33)

In accordance with the determination criterion given by equation (30), the maximum value detector 94 determines, as with the maximum value detector 84 shown in Fig. 11, the maximum value $y'_{n \cdot (k', m(\max))}$ of the correlation statistics $y'_{n \cdot (k', 1)}$, $y'_{n \cdot (k', 2)}$, ..., $y'_{n \cdot (k', M)}$ associated with the user #k in the correlation statistic y' supplied from the mean square error calculator 93. Furthermore, on the basis of a $m(\max)$

at which the maximum value $y'_{n,(k',m(\max))}$ is obtained, the maximum value detector 94 estimates a suboptimum symbol sequence $b'_{n,(k')}$ for the user #k' and outputs it as demodulated data. The maximum value detector 94 also determines and outputs demodulated data for the other users in a similar manner.

In Fig. 13, the correlation matrix calculator 91, the energy estimator 92, and the mean square error calculator 93 form the linear MMSE detector.

Fig. 14 is a flow chart showing the process performed by the UWB demodulator 13 constructed in the form of the suboptimum multi-user demodulator using the linear MMSE detector such as that shown in Fig. 13.

First, in step S21, the correlation matrix calculator 91 determines the correlation matrix R, and the energy estimator 92 determines the energy matrix A. The resultant correlation matrix R and the energy matrix A are supplied to the mean square error calculator 93.

The correlator 21 determines the correlation between the received signal $r(t)$ and the local pulses, and the correlation statistic y obtained as a result is supplied to the mean square error calculator 93. In step S22, the mean square calculator 93 converts the correlation statistic y into a correlation statistic y' in accordance with equation (33) and supplies it to the maximum value detector 94.

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In step S23, the maximum value detector 94 determines the maximum value of the correlation statistic y' supplied from the mean square error calculator 93 for each user in accordance with the determination criterion given by equation (30). Furthermore, on the basis of the maximum value, the maximum value detector 94 estimates a suboptimum symbol sequence b' for each user and outputs it as demodulated data.

Thereafter, the process returns to step S22, and the above-described operation is performed again when the correlation statistic y associated with the next received signal $r(t)$ is supplied from the correlator 21.

Various types of cancellers for canceling interference, such as parallel interference cancellers, successive interference cancellers, and decision feedback cancellers, are described, for example, in the literatures Refs. 10 to 12 or in "Analysis of a simple successive interference cancellation scheme in a DS/CDMA system", by P. Patel and J. M. Holtzman (IEEE J. Select Areas Communications, Vol. 12, pp. 796-807, June 1994 (hereinafter, denoted as Ref. 16)). The principle behind their design is the construction of MAI and its subtraction from the received signal to generate improved symbol decisions on the basis of the correlation matrix. In the case where the UWB demodulator 13 is constructed in the form of a suboptimum multi-user

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That is, in the case where the UWB demodulator 13 is constructed in the form of a suboptimum multi-user demodulator using an interference canceller, the interference canceller 23 may be disposed between the correlator 21 and the symbol detector 22 as represented by a broken line in Fig. 3.

In this case, using all correlation statistics $y_{n'}^{(1)}$, $y_{n'}^{(2)}, \dots, y_{n'}^{(k)}$ outputted from the correlator 21, the interference canceller removes interference components among users (multiple-access interference) from the correlation statistics $y_{n'}^{(1)}, y_{n'}^{(2)}, \dots, y_{n'}^{(k)}$ associated with the respective users, and outputs the result to the symbol detector 22. The symbol detector 22 estimates a suboptimum symbol (sequence) for each user, in accordance with the determination criterion given by equation (30).

As described above, in the present embodiment, the UWB demodulator 13 calculates the correlation between the received signal $r(t)$ corresponding to the signals transmitted from a plurality of users by means of the UWB communication scheme and pulses (local pulses) at possible positions of the transmitted signals from the plurality of users. On the basis of the obtained correlation statistic y ,

and taking into account interference among the signals transmitted from the plurality of users, the received signal $r(t)$ is demodulated into original data issued by the plurality of users. Thus, a high-performance UWB communication demodulator is achieved according to the present embodiment of the invention.

For example, in the DS-CDMA (Direct Sequence CDMA) communication, the processing gain determined by the ratio of the chip rate to the data rate is limited so that the correlation among signals transmitted from users does not become equal to 0. That is, in the CDMA communication, at a transmitting device, data is multiplied by a spread code in one period thereby spreading the spectrum of the data over a wide band. At a receiving device, a received signal is multiplied by the same spread code as that employed at the transmitting device and the resultant product is integrated over one period of the spread code thereby determining the correlation with the received signal. Thus, in the CDMA communication, the correlation between spread codes assigned to different users remains for a long time.

In contrast, in the UWB communication, the processing gain is determined by the bandwidth-to-PRF ratio. Because the bandwidth is very wide as described above, the processing gain becomes large. Thus, there is a high probability that the correlation among signals transmitted

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from different users becomes 0. That is, in the UWB communication, no spread code is used, but data is transmitted using very short pulses which cause the frequency spectrum to be distributed over an ultra wide band. Therefore, in the UWB communication, the correlation in the time domain is localized. Thus, in the UWB communication, the correlation matrix R becomes a sparse matrix (most elements of which are 0). In the correlation matrix R , non-zero elements representing correlations indicate that a collision occurs between pulses, that is, multiple-access interference occurs. The non-zero correlation increases with increasing M indicating the number of chip intervals in a unit symbol period. A reduction in the processing gain and an increase in the number of multiple-access users K (user capacity) also result in an increase in the non-zero correlation.

The dimension of the correlation matrix R increases in proportion to the number of users K and the number of symbols N of a symbol sequence to be estimated. The increase in the dimension of the correlation matrix R results in a great increase in the complexity of the calculation performed by the UWB demodulator 13.

However, if the correlation matrix R is sparse, the correlation matrix R can be divided into lower-dimensional matrices in the calculation. This allows a reduction in the

complexity of the calculation performed by the UWB demodulator 13. For example, in the case where the UWB demodulator 13 includes the interference canceller 23 as shown in Fig. 3, the interference canceller 23 is needed to perform a canceling process only for users among which multiple-access interference can occur on the basis of the TH time $T_n^{(k)}$. This allows a reduction in the complexity of the process.

When the condition $KMT_p < T_s$ is satisfied, symbols #1, #2, ..., #N in a symbol sequence do not have an overlap, at rising-up/falling-down edges, between pulses corresponding to symbols. This makes it unnecessary to deal with a problem caused by overlapping between pulses, and thus, the UWB demodulator 13 is needed to detect not a sequence of symbols but a symbol. That is, when the symbol period satisfies the condition $MT_p < T_s$, any symbol (pulse) of any user is not interfered with by nearby symbols, and thus the correlation statistics associated with the respective users, outputted from the correlator 21, become independent of each other.

In the UWB communication, as described above, unlike the CDMA communication in which the correlation among signals transmitted from different users does not generally become 0, the correlation matrix R becomes sparse, and thus a drastic reduction in the complexity of the process can be

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achieved.

It will be described in more detail below how the sparse form of the correlation matrix R allows a reduction in the complexity of the process performed by the UWB demodulator 13 in UWB multiple-access communication.

The correlation matrix R is given in the form of a symmetric matrix. Therefore, its elements $\rho_{n,k,m}^{n',k',m'}$ given by equation (13) representing the correlations satisfy the condition $\rho_{n,k,m}^{n',k',m'} = \rho_{n',k',m'}^{n,k,m}$.

Herein, we assume that the correlation matrix R consists of $N \times N$ matrices $r_n^{n'}$ as shown in equation (34).

$$R = \begin{bmatrix} r_1^1 & \cdot & \cdot & \cdot & r_N^1 \\ \cdot & \cdot & \cdot & \cdot & \cdot \\ \cdot & \cdot & \cdot & \cdot & \cdot \\ \cdot & \cdot & \cdot & \cdot & \cdot \\ r_1^N & \cdot & \cdot & \cdot & r_N^N \end{bmatrix} \quad (34)$$

In equation (34), each matrix $r_n^{n'}$ is a $KM \times KM$ matrix consisting of elements each representing the correlation between a pulse $a^{(m)}(t - nT_s - T_n^{(k)})$ located in an n th symbol of the received signal $r(t)$ and an n' th local pulse $a^{(m')}(t - n'T_s - T_{n'}^{(k')})$, and the matrix $r_n^{n'}$ can be represented by $K \times K$ matrices $r_{n,k}^{n',k'}$, as shown below.

$$r_n^{n'} = \begin{bmatrix} r_{n,1}^{n',1} & \cdot & \cdot & \cdot & r_{n,K}^{n',1} \\ \cdot & \cdot & \cdot & \cdot & \cdot \\ \cdot & \cdot & \cdot & \cdot & \cdot \\ \cdot & \cdot & \cdot & \cdot & \cdot \\ r_{n,1}^{n',K} & \cdot & \cdot & \cdot & r_{n,K}^{n',K} \end{bmatrix} \quad (35)$$

In equation (35), each matrix $r_{n,k}^{n',k'}$ is an $M \times M$ matrix $r_{n,k,m}^{n',k',m'}$ consisting of elements each representing the correlation between a pulse $a^{(m)}(t - nT_s - T_n^{(k)})$ located in an n th symbol of a user $\#k$ in the received signal $r(t)$ and an n' th local pulse $a^{(m')}(t - n'T_s - T_n^{(k')})$ of a user $\#k'$, and the matrix $r_{n,k}^{n',k'}$ can be represented by $M \times M$ matrices $r_{n,k,m}^{n',k',m'}$ as shown below.

$$r_{n,k}^{n',k'} = \begin{bmatrix} r_{n,k,1}^{n',k',1} & . & . & . & r_{n,k,M}^{n',k',1} \\ . & . & . & . & . \\ . & . & . & . & . \\ . & . & . & . & . \\ r_{n,k,1}^{n',k',M} & . & . & . & r_{n,k,M}^{n',k',M} \end{bmatrix} \quad (36)$$

Of the matrices $r_n^{n'}$ given by equation (35), those matrices whose n and n' satisfy the condition $|n' - n| > 1$ are zero matrices. Therefore, the correlation matrix R given by equation (34) can be represented into the form of a matrix including $N \times N$ matrices as elements, as shown below:

$$R = \begin{bmatrix} r_1^1 & r_2^1 & O_{KM} & O_{KM} & O_{KM} & \cdots & O_{KM} \\ r_1^2 & r_2^2 & r_3^2 & O_{KM} & O_{KM} & \cdots & O_{KM} \\ O_{KM} & r_2^3 & r_3^3 & r_4^3 & O_{KM} & \cdots & O_{KM} \\ \vdots & \ddots & & \ddots & & \ddots & \vdots \\ O_{KM} & \cdots & \cdots & \cdots & O_{KM} & r_{N-1}^N & r_N^N \end{bmatrix} \quad (37)$$

In equation (37), matrix O_x denotes an $x \times x$ zero matrix.

From equation (37), the correlation matrix R becomes a triangular symmetric matrix similar to that described, for example, in "Matrix Computations" 3rd ed., by G. H. Golub

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and C. F. Van Loan (The Johns Hopkins University Press, 1996, pp. 16-17, (hereafter, denoted as "Ref. 17"))).

Herein, the "triangular symmetric matrix" refers to a matrix whose elements are 0 except for diagonal elements and adjacent elements on both sides of diagonal elements. When the correlation matrix R is expressed using matrices $r_n^{n'}$ given by equation (35) as elements, the correlation matrix R becomes a triangular symmetric matrix. In other words, if the correlation matrix R is represented using elements which are all scalar, it does not become a triangular symmetric matrix. In this regard, the correlation matrix R is not a triangular symmetric matrix in the strict sense.

When $k = k'$, elements correspond to symbols from the same user. Because there is no correlation among nearby symbols from the same user, the matrix $r_{n,k}^{n',k'}$ ($= r_{n,k}^{n',k}$) given by equation (36) becomes a zero matrix O_m . In the case where $k = k'$ and $n = n'$, elements correspond to the symbol from the same user. In this case, because pulses at different possible positions for the same symbol are orthogonal to each other, the correlation $\rho_{n,k,m}^{n',k',m'}$ ($= \rho_{n,k,m}^{n,k,m'}$) in equation (14) can be calculated as follows:

$$\rho_{n,k,m}^{n,k,m'} = \begin{cases} 1, & \text{if } m' = m, \\ 0, & \text{otherwise.} \end{cases} \quad (38)$$

Therefore, when $k = k'$ and $n = n'$, the matrix $r_{n,k}^{n',k'}$ given by equation (36) becomes an $M \times M$ unit matrix I_m .

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Herein, I_x denotes an $x \times x$ unit matrix.

Herein, let us assume that the number of users, K , is equal to 3, and symbol detection ($N = 1$) is performed for a received signal modulated by means of binary pulse position modulation (that is, $M = 2$).

Let us further assume that the chip interval T_p in equation (4) is equal to 1.5 ns, the parameter τ_{uwb} in equation (5) is equal to 0.7531, and the symbol transmission interval T_s in equation (2) is greater than $10T_p$. Furthermore, as for the TH time T_n^k in equation (2), it is assumed that $T_1^{(1)} = 0$, $T_1^{(2)} = T_p$, and $T_1^{(3)} = 5T_p$. Still furthermore, the energy of the transmitted signal is identical for all three users #1 to #3.

Under the above conditions, the correlation matrix R can be determined as a 6 ($= 1 \times 3 \times 2$) \times 6 matrix as follows:

$$R = \begin{bmatrix} 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 1 & 1 & 0 & 0 & 0 \\ 0 & 1 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \end{bmatrix} \quad (39)$$

Herein, symbols transmitted from the users #1 to #3 can be determined by means of the maximum-likelihood estimation in accordance with equation (31). That is, in accordance with equation (31), the estimated symbols (vector) b' is

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given by a 6×1 vector as shown below.

$$b' = [b_1^{(1)T}, b_1^{(2)T}, b_1^{(3)T}]^T \quad (40)$$

In equation (40), each element $b_n^{(k)}$ of the vector b' is a $2 (= M) \times 1$ vector.

In the case where the correlation matrix R is given by equation (39), the problem of detecting symbols from the three users #1 to #3 reduces to detecting two symbols as described below.

That is, the correlation matrix R in equation (39) can be divided into four matrices: a 4×4 matrix on the upper left side; a 2×4 matrix on the lower left side; a 4×2 matrix on the upper right side; and a 2×2 matrix on the lower right side, as shown in equation (41). This means that although multiple-access interference occurs between the user #1 and the user #2, the user #3 has no multiple-access interference with the other users.

$$R = \begin{bmatrix} \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 1 & 0 \\ 0 & 1 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} & \begin{bmatrix} 0 & 0 \\ 0 & 0 \\ 0 & 0 \\ 0 & 0 \end{bmatrix} \\ \begin{bmatrix} 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{bmatrix} & \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} \end{bmatrix} \quad (41)$$

Herein, if the 4×4 matrix on the upper right side in equation (41) is denoted by R' and the $x \times y$ zero matrix is denoted by $O_{x,y}$, then the correlation matrix R in equation (41) can be expressed as follows:

$$R = \begin{bmatrix} R' & O_{4,2} \\ O_{2,4} & I_2 \end{bmatrix} \quad (42)$$

From equation (42), the detection of symbols according to equation (31) reduces to detecting symbols from the user #1 and the user #2 between which multiple-access interference occurs and detecting the symbol from the user #3 having no interference with the other users.

Thus, the estimated symbols $[b'_1{}^{(1)}, b'_1{}^{(2)}]$ from the user #1 and the user #2 can be determined on the basis of equation (43) corresponding to equation (31), and the estimated symbol $b'_1{}^{(3)}$ from the user #3 can be determined on the basis of equation (44) corresponding to equation (31).

$$[b_1^{(1)T}, b_1^{(2)T}]^T = \arg \min_{[b_1^{(1)T}, b_1^{(2)T}]^T} \left\| [y_1^{(1)T}, y_1^{(2)T}]^T - R' [b_1^{(1)T}, b_1^{(2)T}]^T \right\|^2 \quad (43)$$

$$b_1^{(3)} = \arg \min_{b_1^{(3)}} \| y_1^{(3)} - I_2 b_1^{(3)} \|^2 \quad (44)$$

In the UWB communication, because the correlation matrix R has a sparse form as described above with reference to, for example, equation (39), the correlation matrix R can be divided (reduced) as shown in equation (42), and thus the calculation cost can be drastically reduced compared with the cost needed when the correlation matrix R is not (cannot be) divided.

In the case where in all N symbols from all users #1 to #K, pulses at M possible positions are orthogonal to each

other, that is, in the case where there is no overlap among pulses, the correlation matrix R becomes an $NKM \times NKM$ unit matrix $I_{n,k,m}$. When the correlation matrix R becomes a unit matrix as in the above-described case, the process performed by the multi-user UWB demodulator 13 becomes equivalent to the process performed by K single-user demodulators.

Figs. 15 and 16 shows the simulated value of the SER (Symbol Error Rate) as a function of E_b/N_0 for the UWB demodulator 13 constructed in the form of an optimum multi-user demodulator (optimum detector).

The simulation shown in Figs. 15 and 16 was performed by means of Monte-Carlo method on the assumption that $M = 2$, $T_p = 1.5$ ns, $\tau_{uwb} = 0.7531$, and the signal energy from any user has an identical value E_s .

In Fig. 15, the number of users, K , is assumed to be 2, and the TH times $T_1^{(1)}$ and $T_1^{(2)}$ are assumed to be 0 and T_p , respectively. Furthermore, in Fig. 15, the symbol transmission period T_s is set so as to satisfy the condition $T_s > KMT_p$ ($= 4T_p$) and thus so that $N = 1$, that is, a symbol is detected. The bit energy E_b is calculated according to $E_b = E_s/\log_2 M$.

In Fig. 15 (and also in Fig. 16), a curve labeled "ML" indicates the SER for the optimum multi-user demodulator, and a curve labeled "CONV" indicates the SER for the single-user demodulator. In the single-user demodulator, as can be

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seen from Fig. 15, no significant improvement in the SER is obtained if the E_b/N_0 is increased, and an error floor due to multiple-access interference occurs. That is, in the single-user demodulator, because multiple-access interference is not taken into account, a pulse placed in the first symbol to transmit data #d from a user #1 and a pulse placed in the first symbol to transmit the same data #d from a user #2 are both detected by the demodulator of the user #1 as a pulse placed in the first symbol from the user #1, even in an ideal environment including no noise. That is, because $M = 2$ in this example, the unit symbol interval is divided into two chip intervals, and a pulse is placed only in one of the two chip intervals. Herein, the T_H times for the user #1 and user #2 are respectively 0 and T_p , and thus the difference between them is equal to the chip interval T_p . As a result, the demodulator of the user #1 detects pulses at both positions in the first symbol. In fact, the simulation indicates that the correlation statistic has the same value for both positions. The detection by the demodulator of the user #2 becomes similar for the second symbol transmitted from the users #1 and #2.

In contrast, in the optimum multi-user demodulator, because the multiple-access interference is taken into account, the SER is improved as the E_b/N_0 increases.

In Fig. 15, a curve labeled "SINGLE-USER" indicates the

lower limit of the SER of the single-user demodulator when there is no multiple-access interference. As can be seen from Fig 15, the SER of the optimum multi-user demodulator is similar to the ideal value, that is, the lower limit of the SER of the single-user demodulator when there is no multiple-access interference.

In Fig. 15 (and also in Fig. 16), the curve labeled "SINGLE-USER" was calculated in accordance with a theoretical expression described in "Digital Communication" by J. G. Proakis (McGraw-Hill, 4th. ed., 2001, p.261 (hereafter, denoted as Ref. 18)). This value is similar to the practical lower limit in the range of $E_b/N_0 > 4\log 2 \approx 4.4$ dB.

The performance of the multi-user demodulator varies depending on the relative value of the TH time t_n^k for respective users. As described above, the time hopping is performed to avoid collisions among users. If there is no pulse collision among users, the performance of the multi-user demodulator becomes similar to the ideal performance obtained by the single-user demodulator when there is no multiple-access interference. That is, in Fig. 15, the SER of the optimum multi-user demodulator indicated by the curve "ML" is similar to the lower limit of the SER of the single-user demodulator indicated by the curve "SINGLE-USER".

On the other hand, when there is perfect collide

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between pulses from different users, such as can occur when the TH times $T_1^{(1)}$ and $T_1^{(2)}$ are both 0 and the pulse position of the user #1 and the pulse position of the user #2 become coincident with each other, the SER of the optimum multi-user demodulator represented by the curve "ML" in Fig. 15 becomes identical to the SER of the single-user demodulator represented by the curve "CONV".

In the simulation shown in Fig. 16, it is assumed that the number of users, K , is equal to 4, and the symbol transmission interval T_s is equal to 10 ns (and thus, the PRF becomes 100 MHz ($= 1/10$ (ns))). In the simulation shown in Fig. 16, the TH time t_n^k is given by a random number.

In Fig. 16, an error floor occurs in the SER for both the optimum multi-user demodulator (indicated by a curve "ML") and the single-user demodulator (indicated by a curve "SINGLE-USER").

However, at $E_b/N_0 = 15$ dB, the SER of the optimum multi-user demodulator (indicated by the curve "ML") is lower than that of the single-user demodulator (indicated by the curve "CONV") by a factor greater than 4.

The above improvement in the SER by a factor greater than 4 is achieved because, in the multi-user demodulator, unlike the single-user demodulator in which demodulation is performed for each user, demodulation is performed jointly for all four users. The improvement in the SER achieved by

the multi-user demodulator, indicated in Fig. 16, is very great.

The processing sequence described above may be executed by hardware or software. When the processes are performed by software, a software program is installed on a general-purpose computer or the like.

Fig. 17 illustrates an embodiment of the invention in which a program used to execute the processes described above is installed on a computer.

The program may be stored, in advance, on a hard disk 105 serving as a storage medium or in a ROM 103 which are disposed inside the computer.

Alternatively, the program may be stored (recorded) temporarily or permanently on a removable storage medium 111 such as a floppy disk, a CD-ROM (Compact Disc Read Only Memory), an MO (Magnetooptical) disk, a DVD (Digital Versatile Disc), a magnetic disk, or a semiconductor memory. Such a removable recording medium 111 may be provided in the form of so-called package software.

Instead of installing the program from the removable recording medium 111 onto the computer, the program may also be transferred to the computer from a download site via a digital broadcasting satellite by means of radio transmission or via a network such as an LAN (Local Area Network) or the Internet by means of wire communication. In

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this case, the computer receives, using a communication unit 108, the program transmitted in such a manner and installs the program on the hard disk 105 disposed in the computer.

The computer includes a CPU (Central Processing Unit) 102. When a user inputs a command by operating an input device 107 such as a keyboard or a mouse connected to the CPU 101 via a bus 101, the command is transferred to the CPU 102 via the input/output interface 110. In accordance with the command, the CPU 102 executes a program stored in the ROM (Read Only Memory) 103. Alternatively, the CPU 102 may execute a program loaded in a RAM (Random Access Memory) 104 wherein the program may be loaded into the RAM 104 by transferring a program stored on the hard disk 105 into the RAM 104, or transferring a program which has been installed on the hard disk 105 after being received from a satellite or a network via the communication unit 108, or transferring a program which has been installed on the hard disk 105 after being read from a removable recording medium 111 loaded on a drive 109, thereby performing the process described above with reference to the flow charts and the block diagram. The CPU 102 outputs the result of the process, as required, to an output device such as an LCD (Liquid Crystal Display) or a loudspeaker via an input/output interface 110. The result of the process may also be transmitted via the communication unit 108 or may be

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Year	1990	1991	1992	1993	1994	1995	1996	1997	1998	1999	2000	2001	2002	2003	2004	2005	2006	2007	2008	2009	2010	2011	2012	2013	2014	2015	2016	2017	2018	2019	2020	2021	2022	2023	2024	2025	2026	2027	2028	2029	2030	2031	2032	2033	2034	2035	2036	2037	2038	2039	2040	2041	2042	2043	2044	2045	2046	2047	2048	2049	2050	2051	2052	2053	2054	2055	2056	2057	2058	2059	2060	2061	2062	2063	2064	2065	2066	2067	2068	2069	2070	2071	2072	2073	2074	2075	2076	2077	2078	2079	2080	2081	2082	2083	2084	2085	2086	2087	2088	2089	2090	2091	2092	2093	2094	2095	2096	2097	2098	2099
1990	1991	1992	1993	1994	1995	1996	1997	1998	1999	2000	2001	2002	2003	2004	2005	2006	2007	2008	2009	2010	2011	2012	2013	2014	2015	2016	2017	2018	2019	2020	2021	2022	2023	2024	2025	2026	2027	2028	2029	2030	2031	2032	2033	2034	2035	2036	2037	2038	2039	2040	2041	2042	2043	2044	2045	2046	2047	2048	2049	2050	2051	2052	2053	2054	2055	2056	2057	2058	2059	2060	2061	2062	2063	2064	2065	2066	2067	2068	2069	2070	2071	2072	2073	2074	2075	2076	2077	2078	2079	2080	2081	2082	2083	2084	2085	2086	2087	2088	2089	2090	2091	2092	2093	2094	2095	2096	2097	2098	2099	

As described above, the communication device, the communication method, and the program according to the present invention have great advantages. That is, the correlation is calculated between the received signal corresponding to the signals transmitted from a plurality of communication terminals by means of UWB (Ultra WideBand) communication technology and pulses at possible positions in the transmitted signals from the respective communication terminals, and the received signal is demodulated into original data issued by the communication terminals on the

項目	1990年	1991年	1992年	1993年	1994年	1995年	1996年	1997年	1998年	1999年	2000年	2001年	2002年	2003年	2004年	2005年	2006年	2007年	2008年	2009年	2010年	2011年	2012年	2013年	2014年	2015年	2016年	2017年	2018年	2019年	2020年	2021年	2022年	2023年	2024年	2025年	2026年	2027年	2028年	2029年	2030年	2031年	2032年	2033年	2034年	2035年	2036年	2037年	2038年	2039年	2040年	2041年	2042年	2043年	2044年	2045年	2046年	2047年	2048年	2049年	2050年	2051年	2052年	2053年	2054年	2055年	2056年	2057年	2058年	2059年	2060年	2061年	2062年	2063年	2064年	2065年	2066年	2067年	2068年	2069年	2070年	2071年	2072年	2073年	2074年	2075年	2076年	2077年	2078年	2079年	2080年	2081年	2082年	2083年	2084年	2085年	2086年	2087年	2088年	2089年	2090年	2091年	2092年	2093年	2094年	2095年	2096年	2097年	2098年	2099年	2100年																																																																		
人口総数	12,000,000	12,500,000	13,000,000	13,500,000	14,000,000	14,500,000	15,000,000	15,500,000	16,000,000	16,500,000	17,000,000	17,500,000	18,000,000	18,500,000	19,000,000	19,500,000	20,000,000	20,500,000	21,000,000	21,500,000	22,000,000	22,500,000	23,000,000	23,500,000	24,000,000	24,500,000	25,000,000	25,500,000	26,000,000	26,500,000	27,000,000	27,500,000	28,000,000	28,500,000	29,000,000	29,500,000	30,000,000	30,500,000	31,000,000	31,500,000	32,000,000	32,500,000	33,000,000	33,500,000	34,000,000	34,500,000	35,000,000	35,500,000	36,000,000	36,500,000	37,000,000	37,500,000	38,000,000	38,500,000	39,000,000	39,500,000	40,000,000	40,500,000	41,000,000	41,500,000	42,000,000	42,500,000	43,000,000	43,500,000	44,000,000	44,500,000	45,000,000	45,500,000	46,000,000	46,500,000	47,000,000	47,500,000	48,000,000	48,500,000	49,000,000	49,500,000	50,000,000	50,500,000	51,000,000	51,500,000	52,000,000	52,500,000	53,000,000	53,500,000	54,000,000	54,500,000	55,000,000	55,500,000	56,000,000	56,500,000	57,000,000	57,500,000	58,000,000	58,500,000	59,000,000	59,500,000	60,000,000	60,500,000	61,000,000	61,500,000	62,000,000	62,500,000	63,000,000	63,500,000	64,000,000	64,500,000	65,000,000	65,500,000	66,000,000	66,500,000	67,000,000	67,500,000	68,000,000	68,500,000	69,000,000	69,500,000	70,000,000	70,500,000	71,000,000	71,500,000	72,000,000	72,500,000	73,000,000	73,500,000	74,000,000	74,500,000	75,000,000	75,500,000	76,000,000	76,500,000	77,000,000	77,500,000	78,000,000	78,500,000	79,000,000	79,500,000	80,000,000	80,500,000	81,000,000	81,500,000	82,000,000	82,500,000	83,000,000	83,500,000	84,000,000	84,500,000	85,000,000	85,500,000	86,000,000	86,500,000	87,000,000	87,500,000	88,000,000	88,500,000	89,000,000	89,500,000	90,000,000	90,500,000	91,000,000	91,500,000	92,000,000	92,500,000	93,000,000	93,500,000	94,000,000	94,500,000	95,000,000	95,500,000	96,000,000	96,500,000	97,000,000	97,500,000	98,000,000	98,500,000	99,000,000	99,500,000	100,000,000